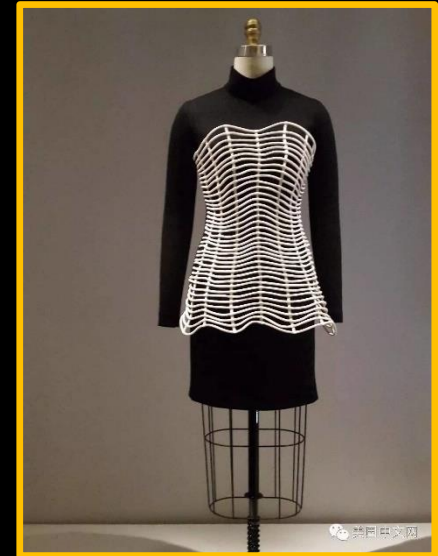
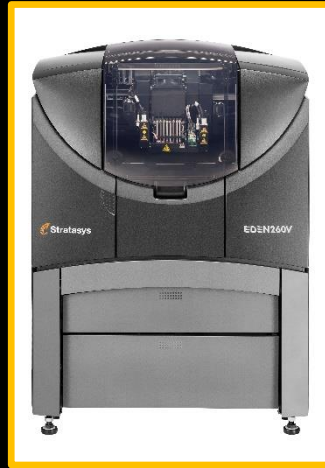
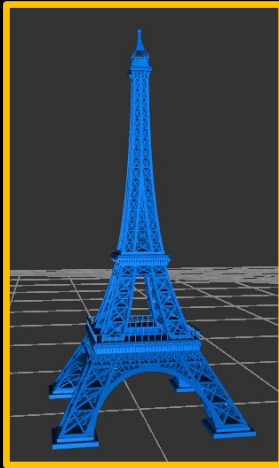


# Computing Interior Support-free Structure via Hollow-to-Fill Construction

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University of Science and Technology of China

# 3D Printing



# Shape optimization



# Prior work – shape optimization



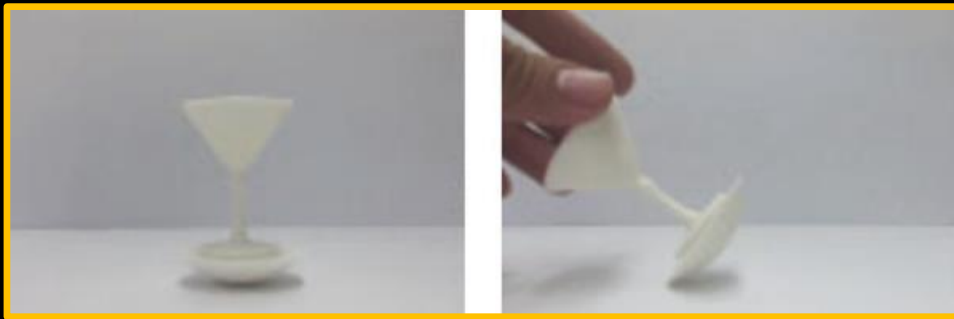
[Prévost et al. 2013]



[Bächer et al. 2014]



[Wang et al. 2016]

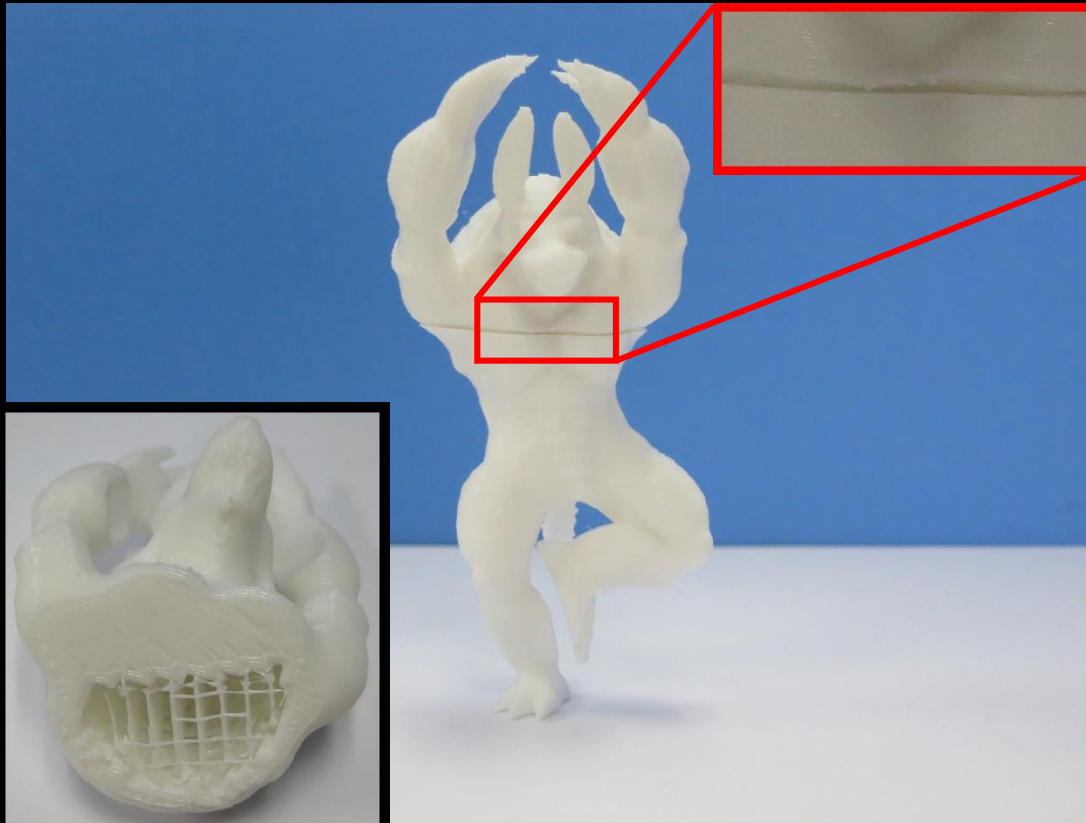


[Zhao et al. 2016]



[Prévost et al. 2016]

# Motivation I



## **Limitation:**

1. The additional interior support structures should be removed.
2. The seam affects the visual beauty.

The printed Armadillo has a seam.  
[Prévost et al. 2013]

# Prior work – support structures



[Chen et al. 2013]



[Vanek et al. 2014]



[Dumas et al. 2014]



[Hu et al. 2015]



[Hu et al. 2015]

CAD/Graphics 2017



[Wu et al. 2016]

August 25, 2017



# Motivation II



The printed cross section of  
the Dilo model [Wu et al. 2016]

## **Limitation:**

The limited rhombic space may lead to more redundant material.

# Goal

Output: Objects have support-free inner surfaces and  
Input: 3D model  
meet the design requirements



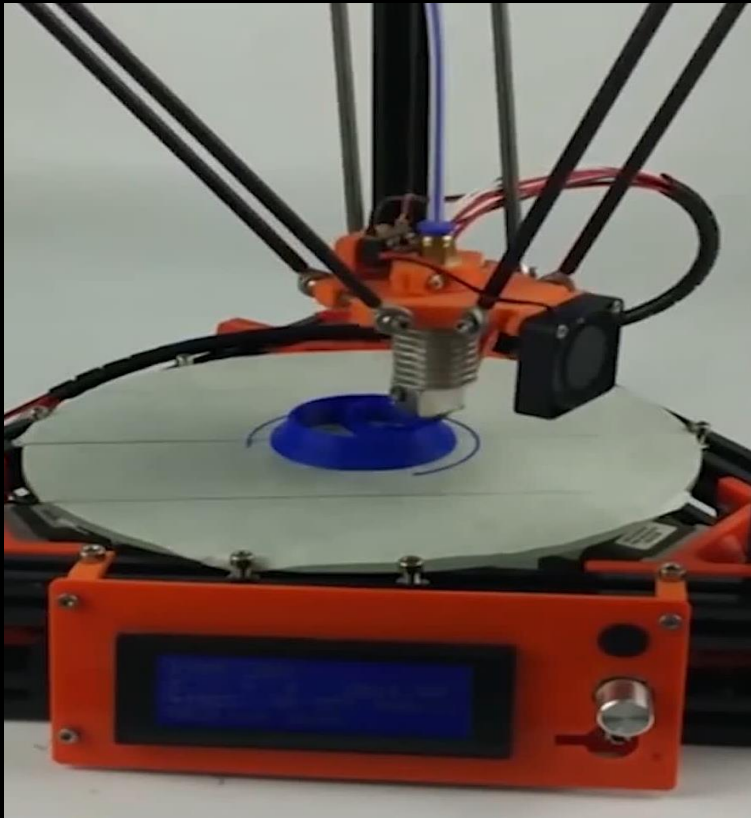
Outer surface  $\mathcal{M}_O$

Inner surface  $\mathcal{M}_I$



# Our Approach

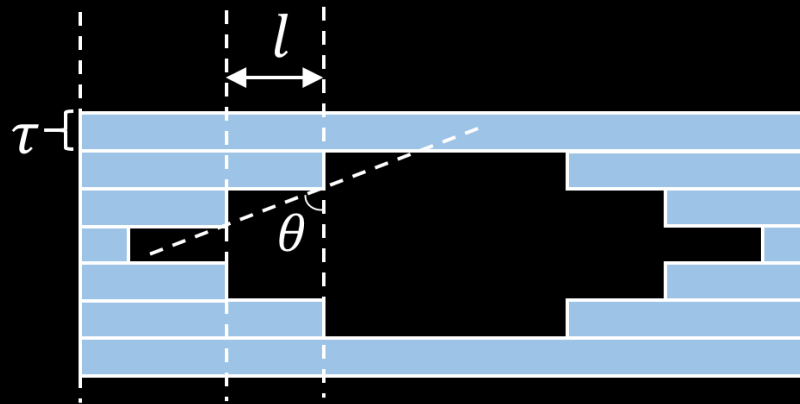
# Fused Deposition Modeling (FDM)



1. Layer by layer.
2. The upper layer should be supported by the lower layer.

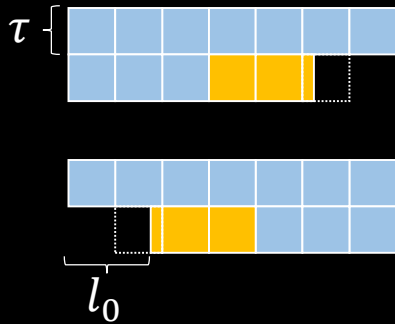
# Support-free condition

- Overhang-angle condition
  - The overhang angle  $\theta \leq \theta_0$ 
    - $\theta_0$ , the maximal overhang-angle
  - The overhang length  $l \leq l_0$ 
    - $l_0$ , the maximal overhang-length

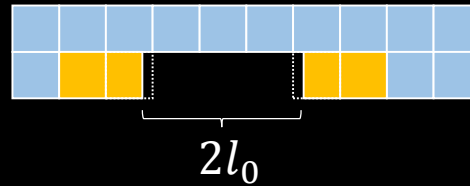


# Types of support-free structures

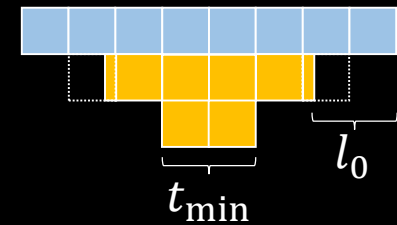
- Three types of support-free structures and the corresponding filling strategy



Type I

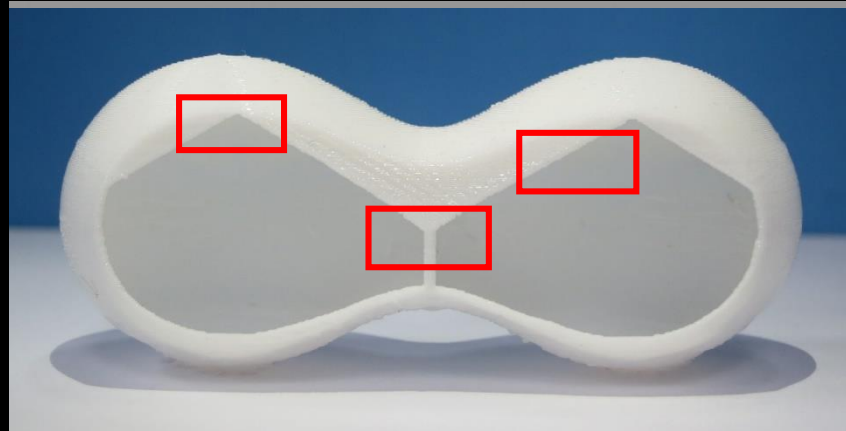


Type II



Type III

# Printed support-free structures



Type I



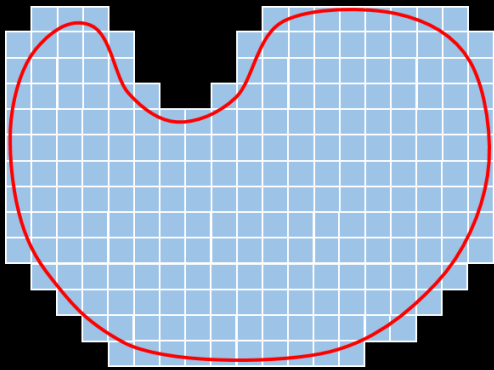
Type II



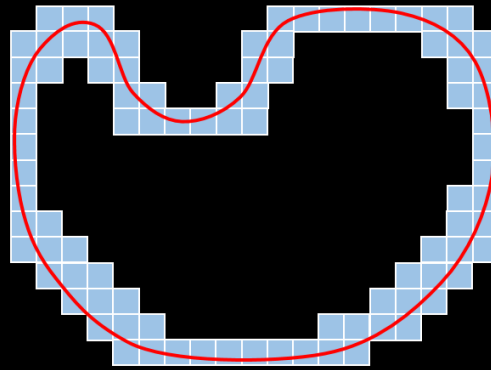
Type III

# Interior support-free structure generation

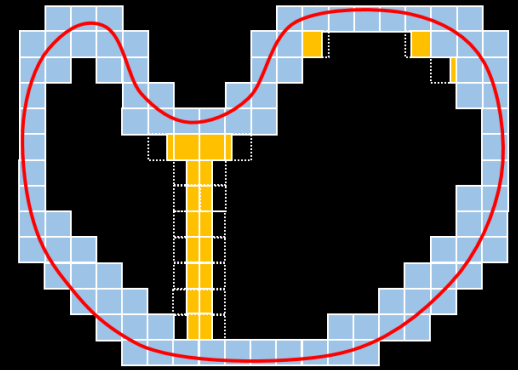
- Hollow-to-fill strategy



A voxelized model



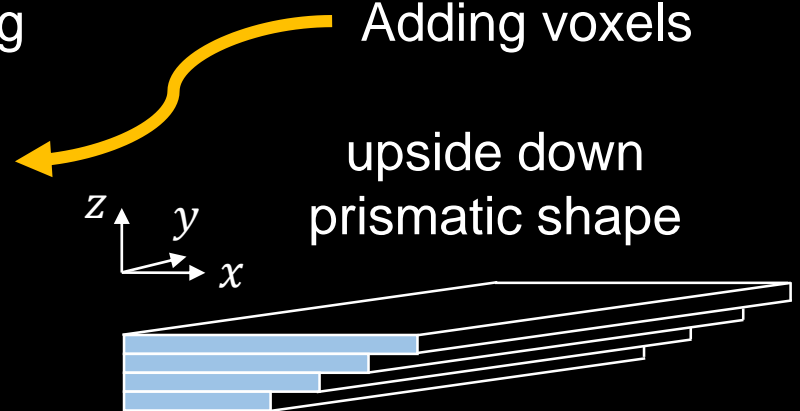
Hollowing



Adding voxels

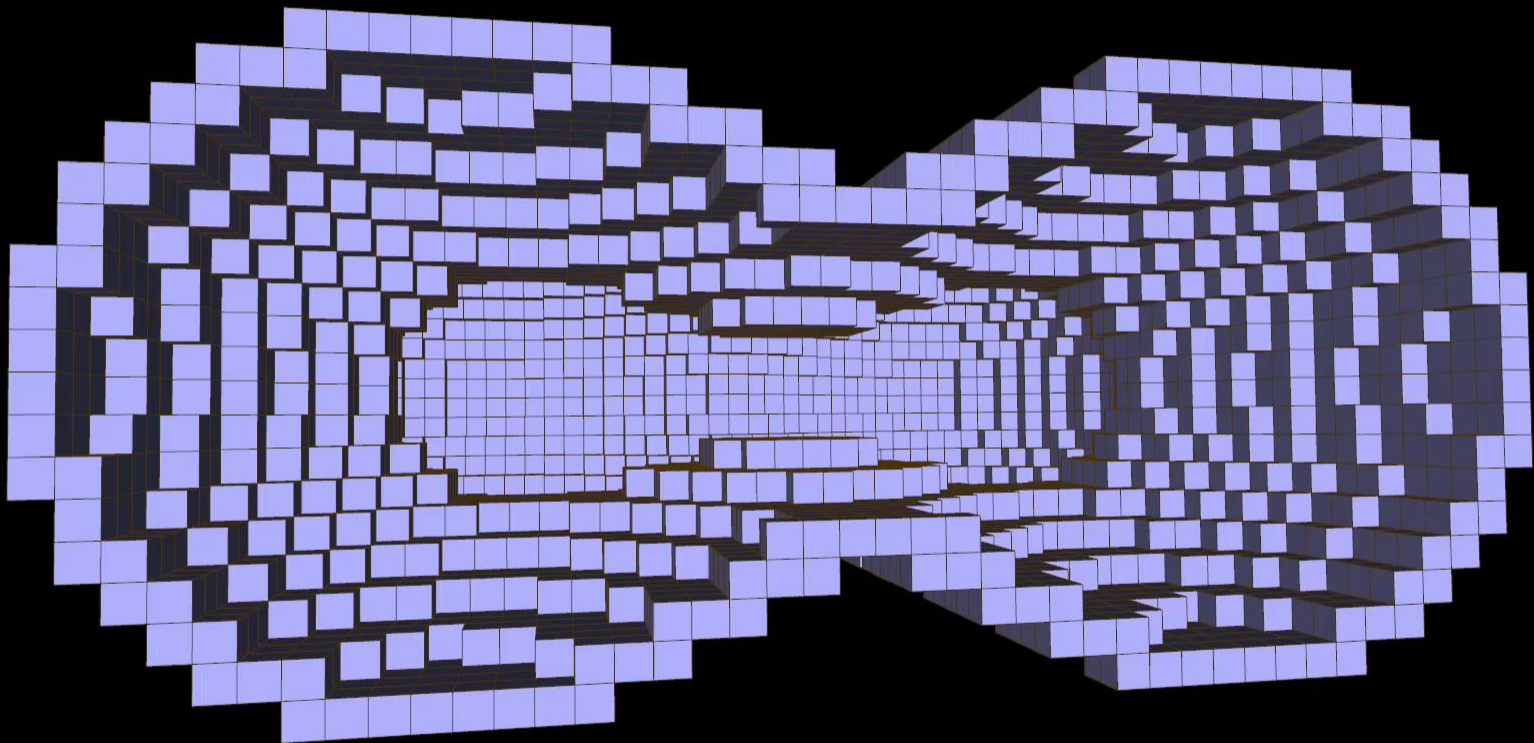
- Greedy voxel-filling strategy

- Layer by layer
- From top to bottom





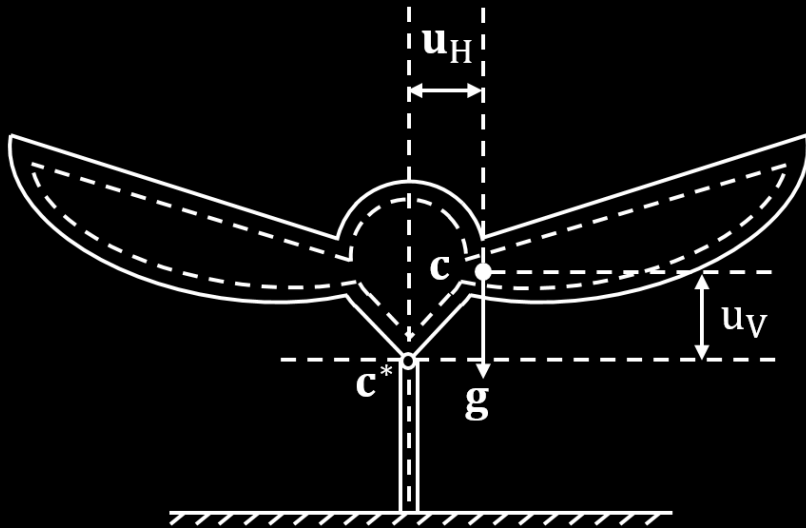
# Interior support-free structure generation



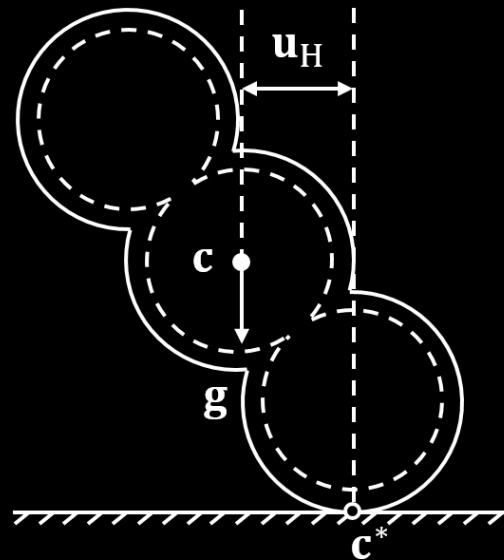
# Applications

# Balanced object design

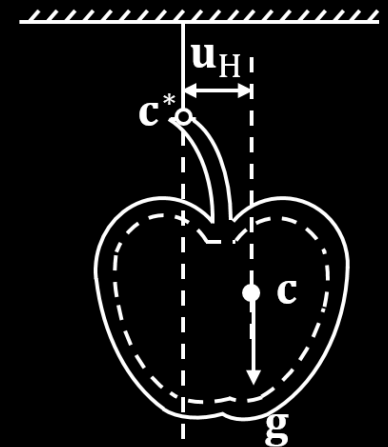
- Three modes of balancing



Standing on a pivot point



Standing on the plane



Suspended

# Problem formulation

$$\min_{\mathcal{M}_O, \mathcal{M}_I} \|\mathbf{u}_H(\mathcal{M}_O, \mathcal{M}_I)\|^2 + \alpha E_d(\mathcal{M}_O) + \beta E_s(\mathcal{M}_O, \mathcal{M}_I)$$

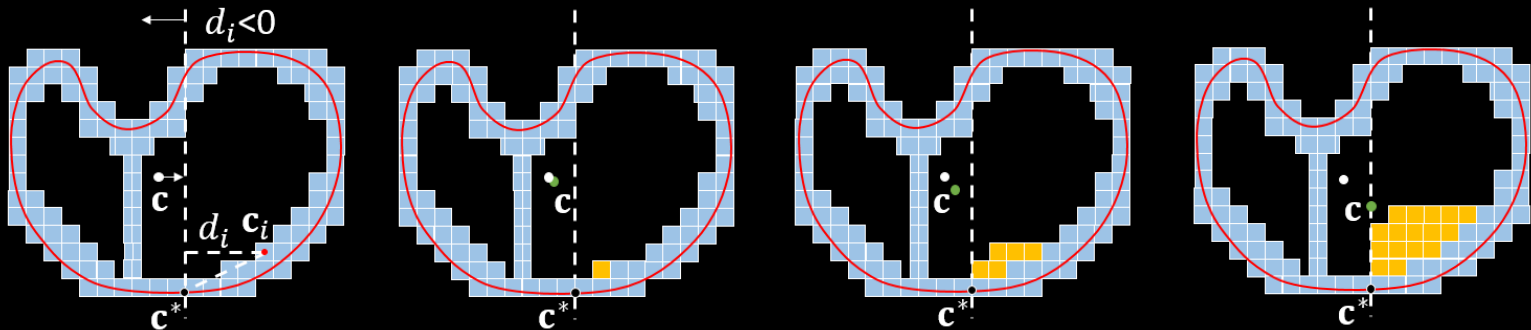
Does it balance?

Does it look like  
the initial shape?

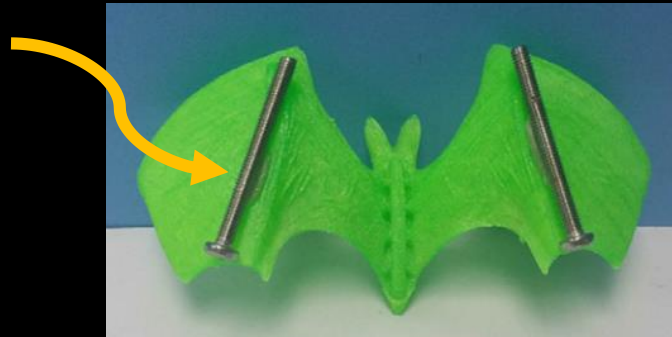
Penalize the  
negative  $u_V$  for  
the first mode  
of balancing.

# Optimization method

- Voxel filling



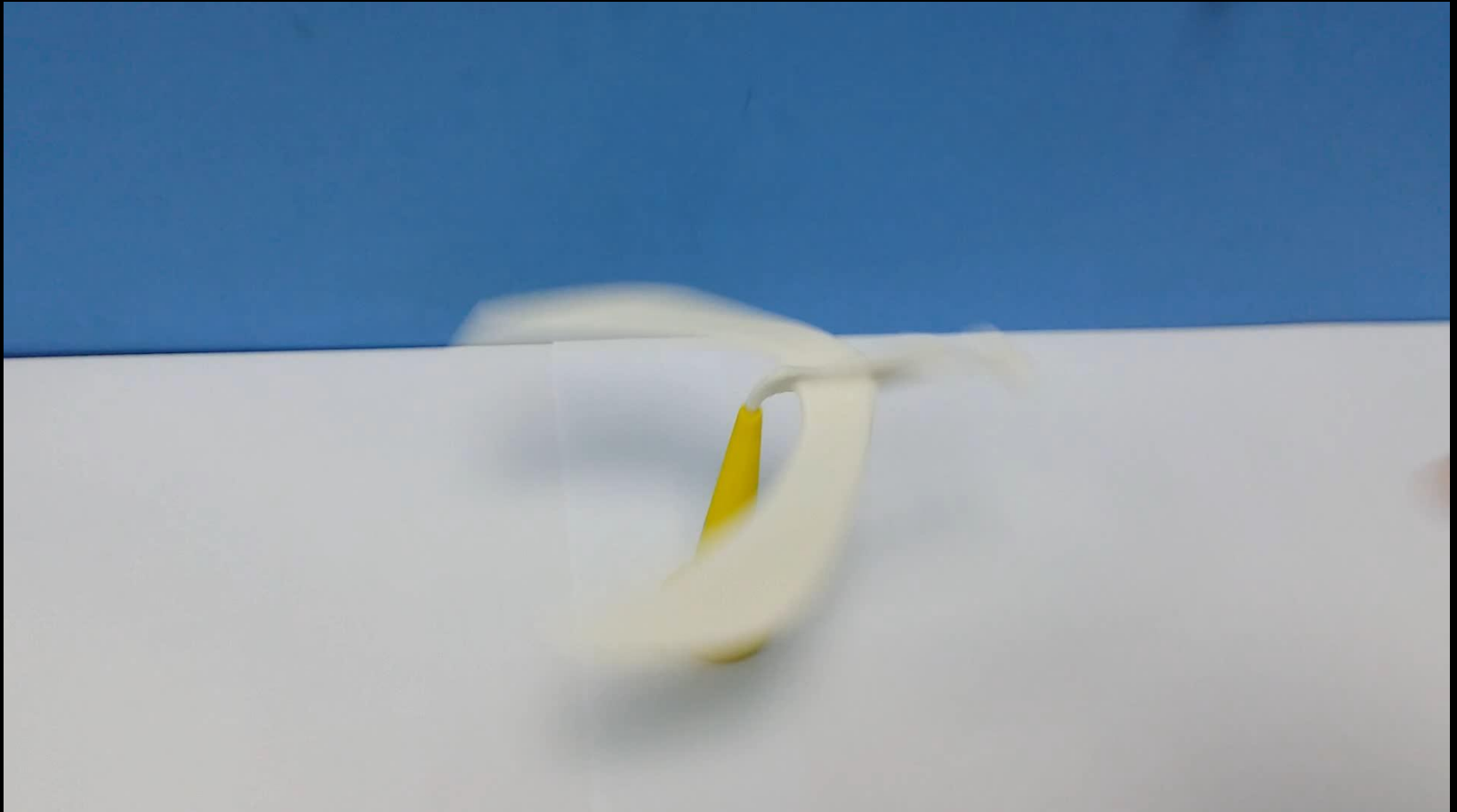
- Model deformation [Prévost et al. 2013]
- Extra weights



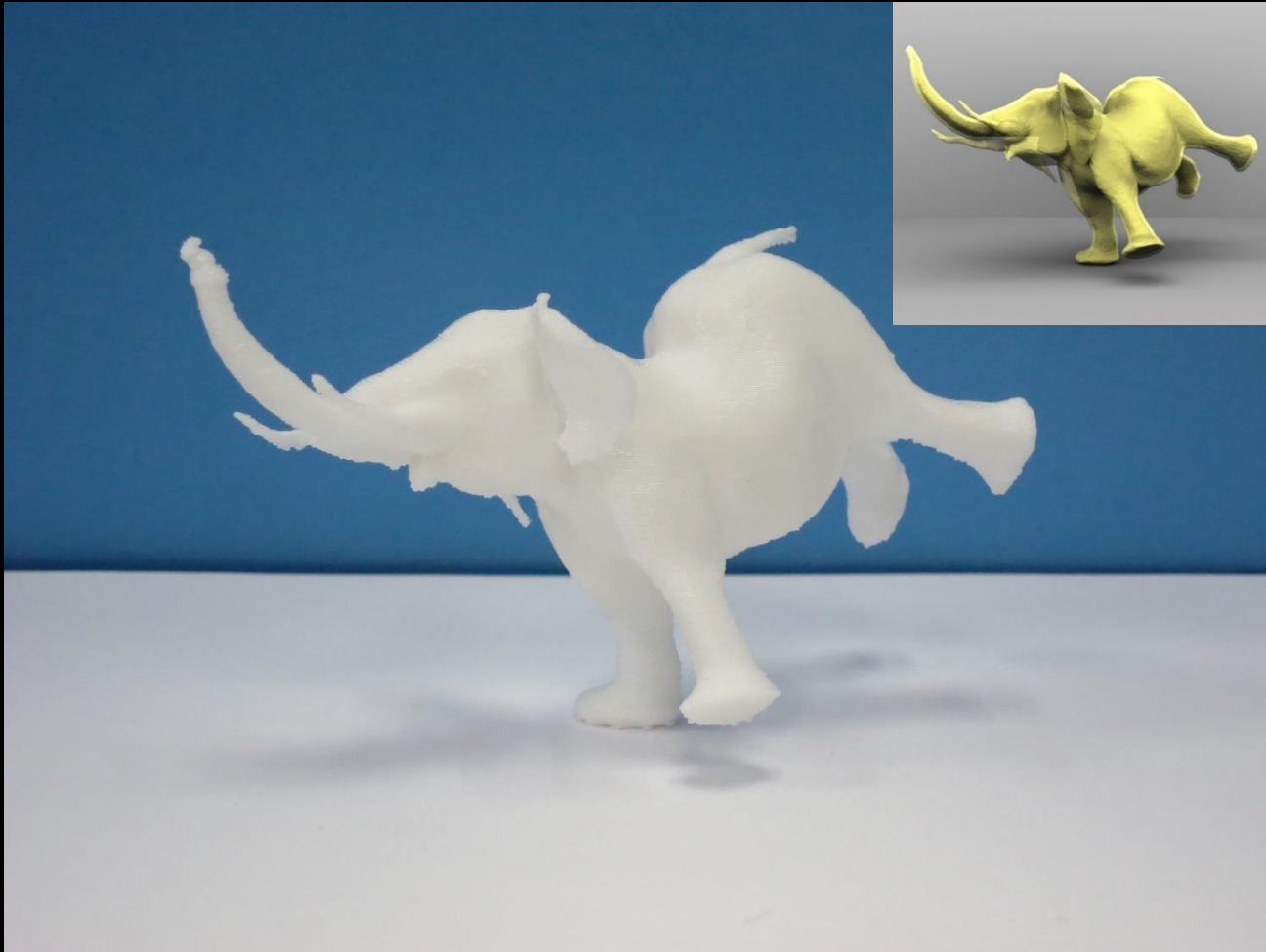
# Results



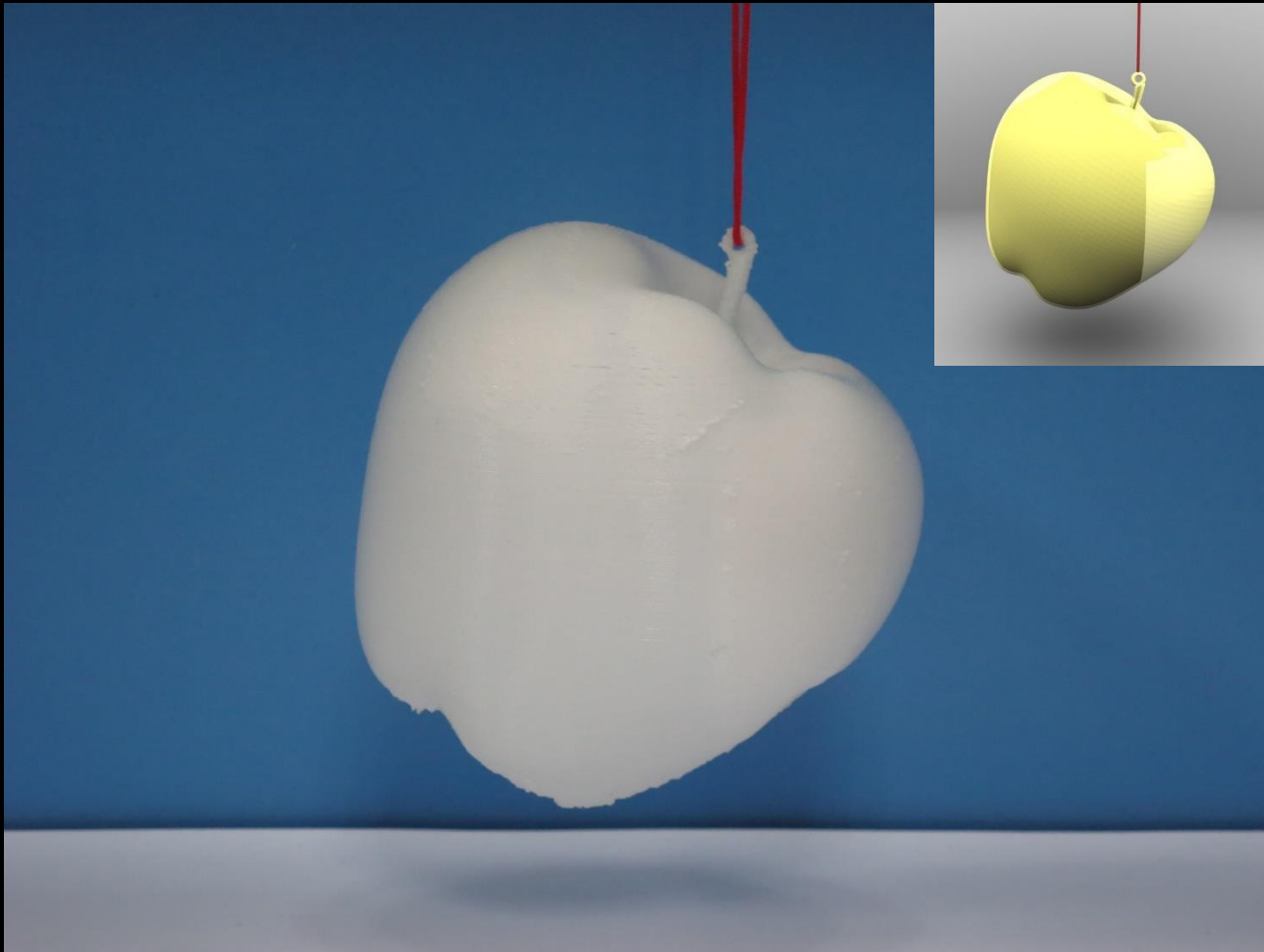
# Balancing bird standing on a pivot



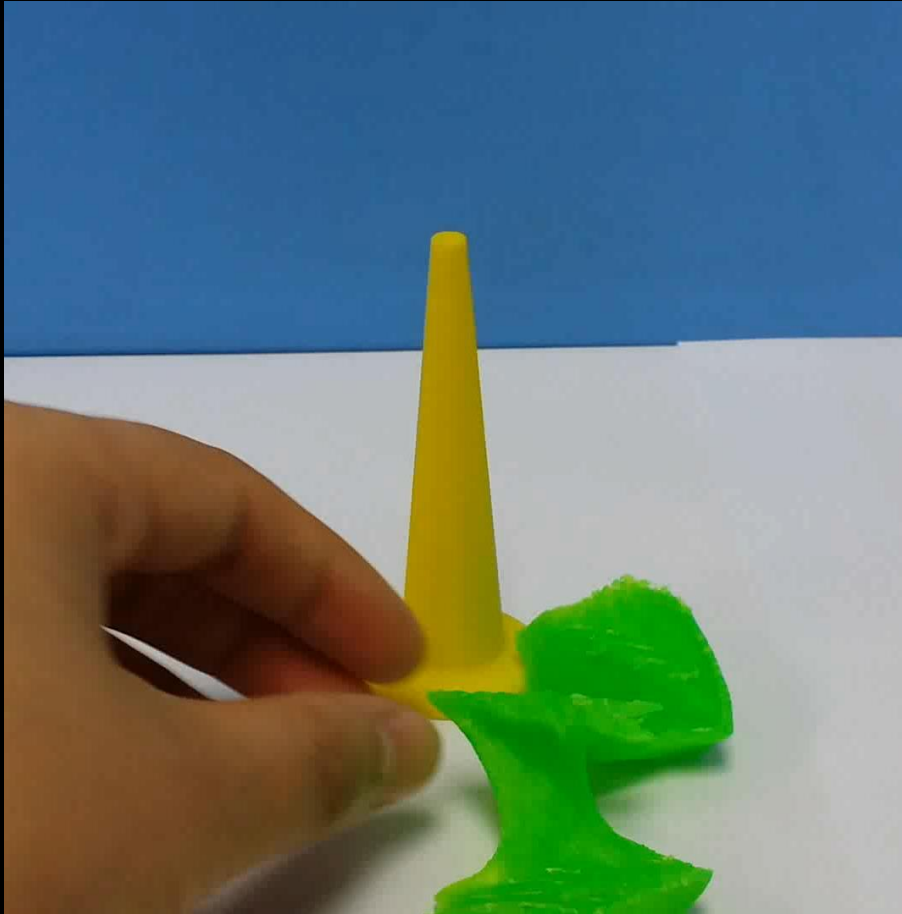
# Balancing elephant standing on the plane



# Suspended balancing apple



# Balancing bat with extra weights



# Comparison with [Wu et al. 2016]

Rhombic structure  
[Wu et al. 2016]

Ours

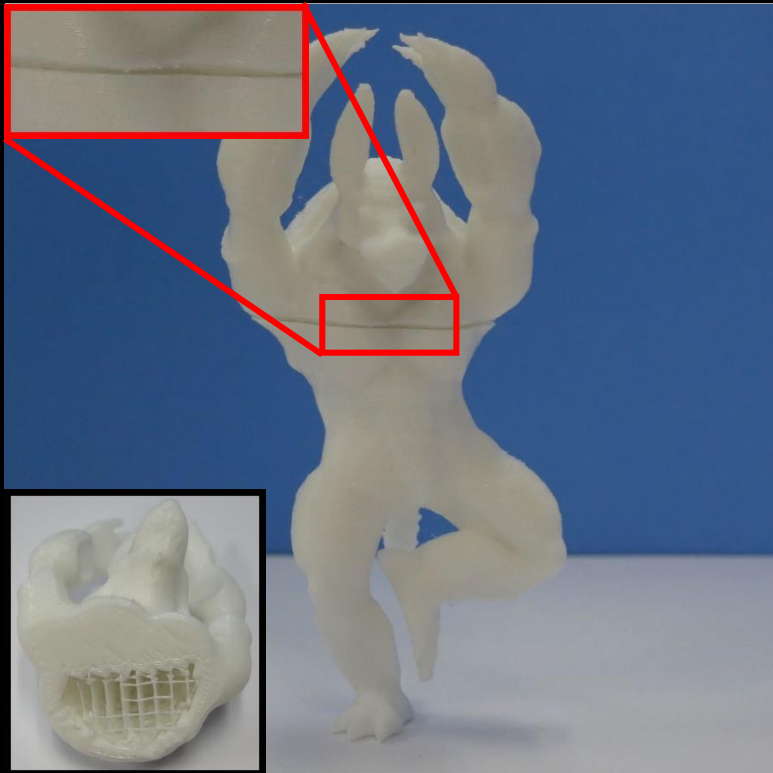


Volume:  $1.011 \times 10^5 \text{ mm}^3$

Volume:  $0.335 \times 10^5 \text{ mm}^3$

# Comparison with [Prévost et al. 2013]

Make It Stand  
[Prévost et al. 2013]



Ours





# Conclusion

- We propose a novel hollow-to-fill strategy to compute interior support-free structures for 3D printing.
- Limitation and future work
  - Limited by the voxel representation
  - Stress analysis
  - Bijective volumetric deformation

*Thank you!*