

Item Response Ranking for Cognitive Diagnosis

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Introduction

Cognitive diagnosis, a fundamental task in education area, aims at providing an approach to reveal the proficiency level of students on knowledge concepts. Actually, **monotonicity is one of the basic conditions in cognitive diagnosis theory**, which assumes that student's proficiency is monotonic with the probability of giving the right response to a test item.

Exercise	Knowledge Concepts	Ada	Bob
e_1	A	✓	✗
e_2	B	✓	✓
e_3	A, B	✗	✗
e_4	C, D	?	✓
e_5	C, E	✗	?

Legend	
A: Function	D: Coordinates
B: Derivative	E: Equation
C: Geometry	
✓ Correct	✗ Wrong

Problem Statement

Given

- N students: $S = \{s_1, s_2, \dots, s_N\}$
- M test items: $E = \{e_1, e_2, \dots, e_M\}$
- L knowledge concepts: $K = \{k_1, k_2, \dots, k_L\}$
- Response logs $\mathcal{R} = \{(s, e, r)\}$
- Q-matrix $Q = \{Q_{ij}\}_{M \times L}$

Goal

Mine students' proficiency on knowledge concepts

Item Response Ranking

Monotonicity

In the literature, the monotonicity theory assumes that student's proficiency is monotonic with the probability of giving the right response to a test item.

$$r_{ie} \leftarrow P(y_{ie})$$

Pairwise Monotonicity

Given a specific test item, the students with right responses are more skilled than those with wrong responses.

$$(r_{ie} - r_{je}) \leftarrow P(y_{ie} - y_{je})$$

Experiments

Statistics	ASSISTments	MATH
# users	4,163	10,268
# items	17,746	917,495
# knowledge concepts	123	1,488
# response logs	324,572	864,722

Table 1: The statistics of the dataset.

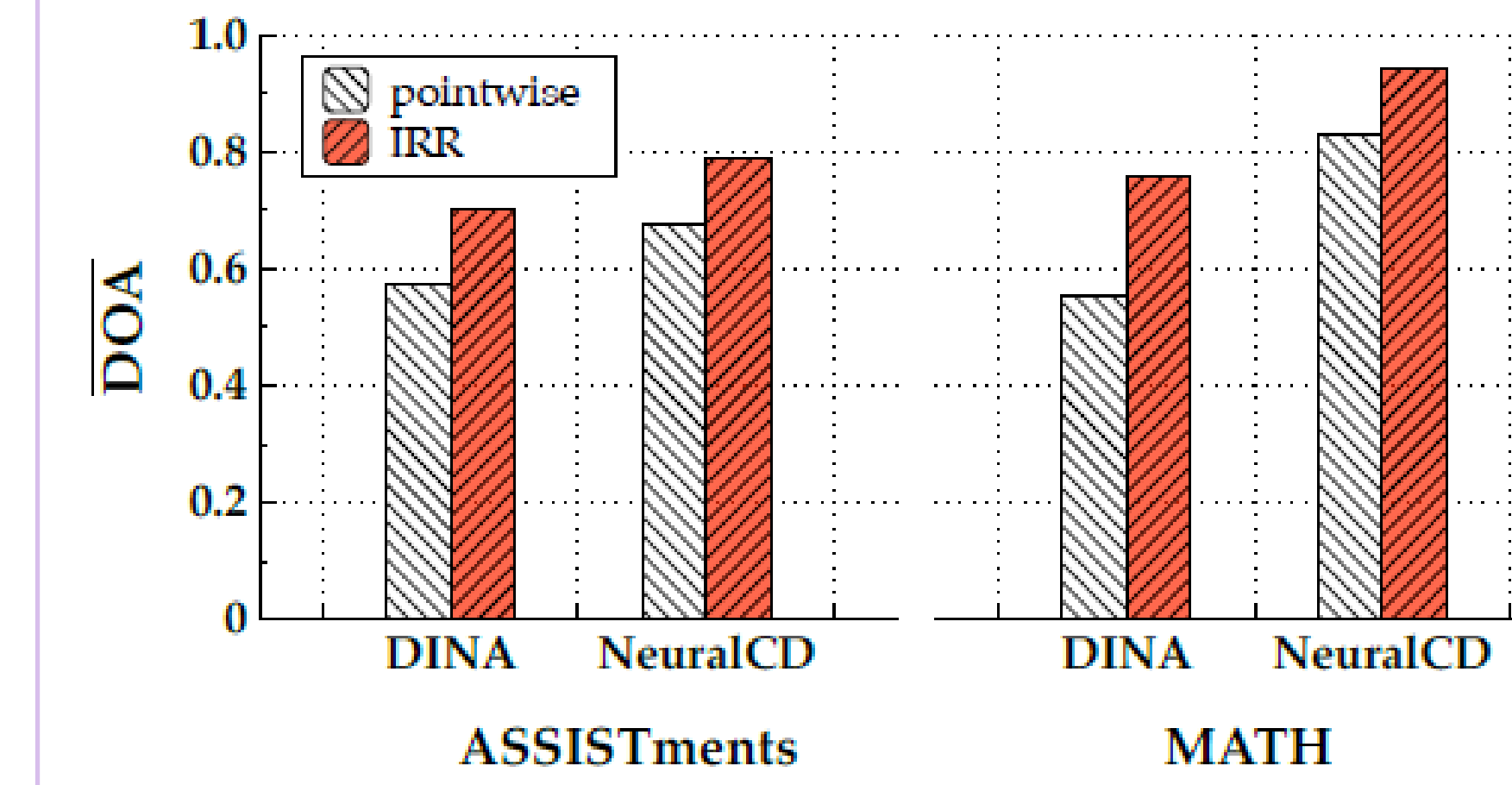


Figure 3: Results of knowledge proficiency estimation.

Metrics		DINA		IRT		MIRT		NeuralCD	
		Pointwise	IRR	Pointwise	IRR	Pointwise	IRR	Pointwise	IRR
Classification	AUC	0.786	0.815	0.776	0.848	0.777	0.889	0.817	0.839
	Precision	0.689	0.713	0.665	0.752	0.716	0.785	0.706	0.734
	Recall	0.485	0.553	0.585	0.607	0.737	0.645	0.662	0.579
	F1	0.518	0.598	0.534	0.654	0.666	0.697	0.625	0.626
Ranking	MAP(E)	0.840	0.853	0.817	0.913	0.824	0.937	0.867	0.907
	NDCG@5(E)	0.871	0.881	0.867	0.894	0.868	0.912	0.881	0.889
	MAP(U)	0.780	0.799	0.754	0.880	0.761	0.908	0.826	0.875
	NDCG@5(U)	0.464	0.481	0.462	0.503	0.462	0.524	0.487	0.500

(a) ASSISTments

Metrics		DINA		IRT		MIRT		NeuralCD	
		Pointwise	IRR	Pointwise	IRR	Pointwise	IRR	Pointwise	IRR
Classification	AUC	0.549	0.567	0.537	0.666	0.537	0.686	0.596	0.608
	Precision	0.717	0.725	0.637	0.760	0.583	0.767	0.686	0.737
	Recall	0.447	0.707	0.722	0.743	0.699	0.750	0.655	0.719
	F1	0.500	0.711	0.524	0.747	0.588	0.754	0.602	0.724
Ranking	MAP(E)	0.735	0.740	0.728	0.808	0.729	0.814	0.765	0.772
	NDCG@5(E)	0.852	0.855	0.845	0.906	0.844	0.909	0.853	0.866
	MAP(U)	0.356	0.360	0.345	0.494	0.347	0.508	0.431	0.437
	NDCG@5(U)	0.488	0.498	0.479	0.654	0.477	0.677	0.587	0.569

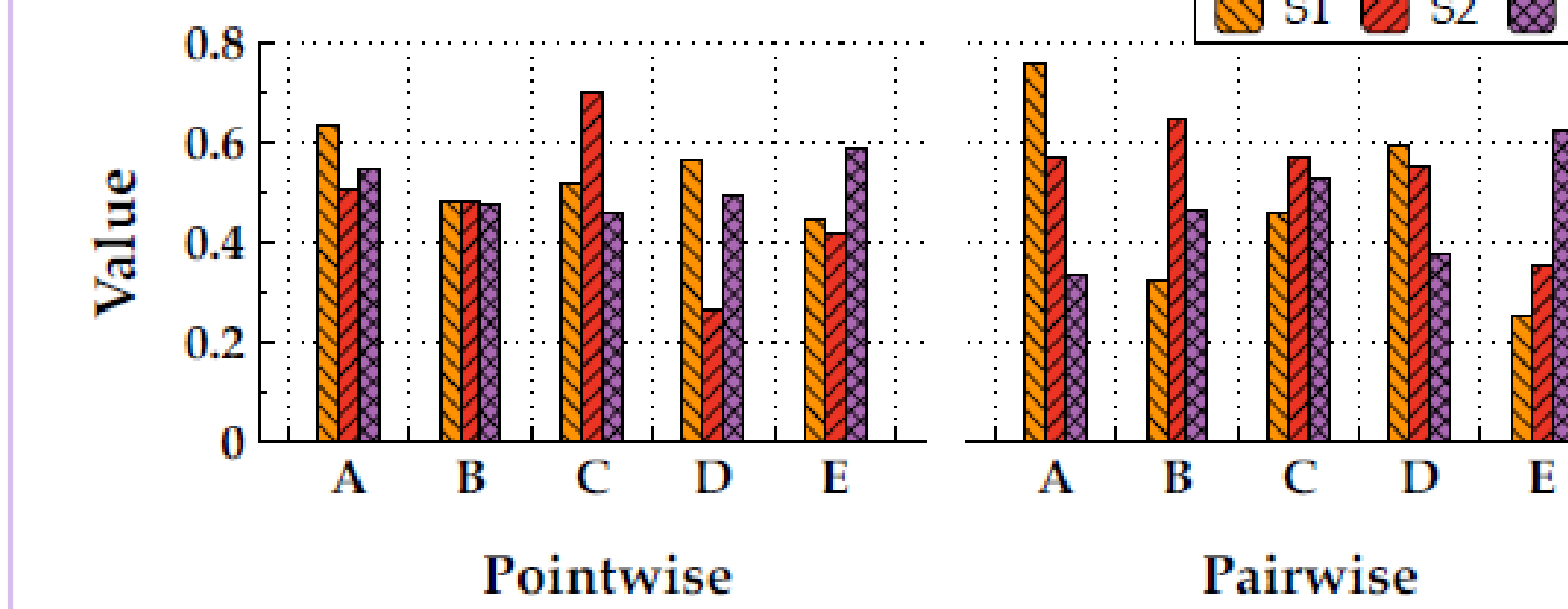
(b) MATH

Table 2: Experimental results on student performance prediction.

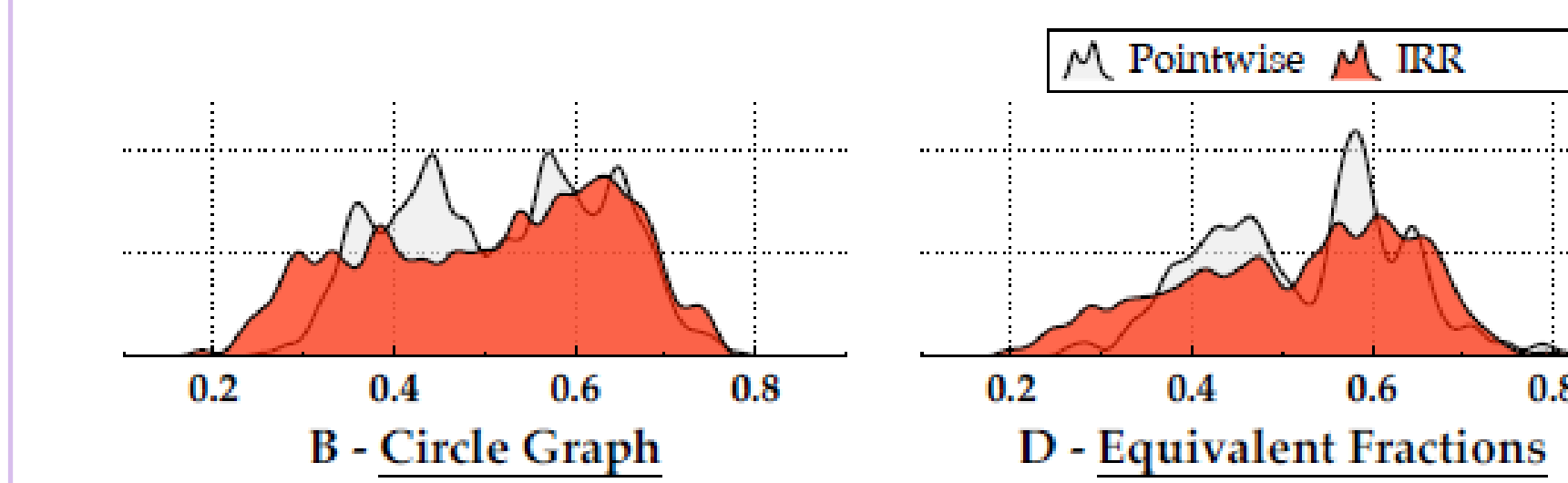
ID	Concepts	Student 1	Student 2	Student 3
Item 1	B, C	✗	✓	✗
Item 2	B, C, D, E	✗	✓	✓
Item 3	A, B, D	✓	✗	✗

A - Proportion	B - Circle Graph	C - Percent Of
D - Equivalent Fractions	E - Finding Percents	

(a) Response Logs diagram.



(b) Proficiency on knowledge concepts diagram.



(c) Proficiency distribution diagram.

Figure 4: An example of diagnostic results.

Pair Construction

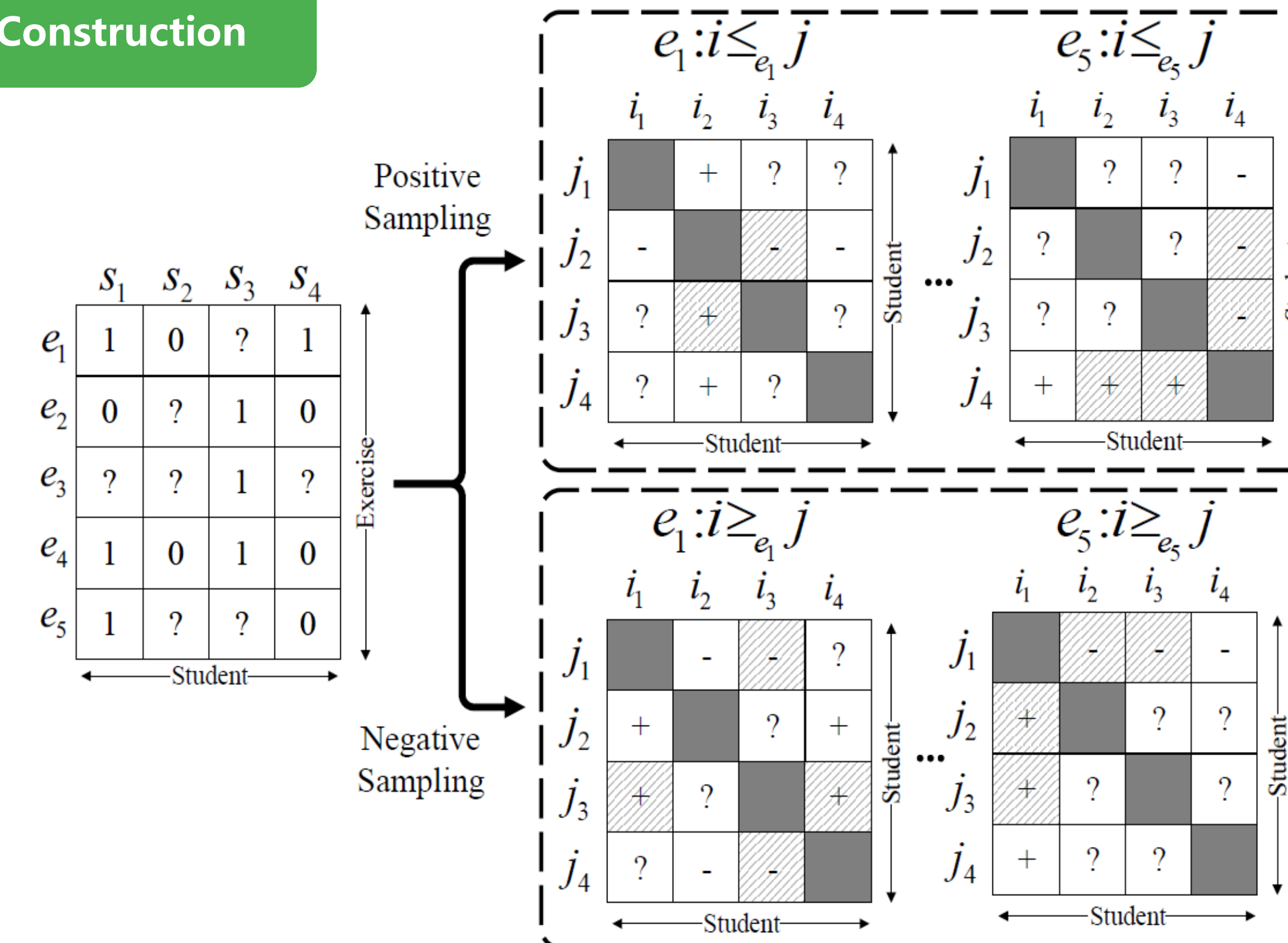


Figure 2: The observed responses are shown on the left part. Our method creates item specific pairwise partial responses $i \geq e_j$ and $i \leq e_j$ between a pair of students. On the right part, (+) indicates the partial order from i to j and (-) vice versa. The striped blocks highlight the pairs containing unobserved responses.

Objective Function

$$\mathcal{L} = - \sum_{(i,j) \in T(R)} \log \frac{\exp(P(r_{ie}|\theta))}{\exp(P(r_{ie}|\theta)) + \exp(P(r_{je}|\theta))} + \lambda(\theta)$$

Observation

Ada with a right response to item e_1 is considered as having a higher proficiency level on the related concept A (i.e., Function) than Bob with a wrong response.

Induction

Students with correct responses should be more proficient than students with wrong responses.

Motivation

Based on the partial order between item responses, we can create a new optimization criteria to exploit the response pairs to enhance the monotonicity.

Key Problem

How to exploit the partial order between responses to improve the monotonicity within the optimization criteria.

Challenges

- It is hard for us to compare item responses across different items related to non-overlapped concepts.
- There exist many unobserved responses.
- How to find an objective function so that the monotonicity can be directly optimized