- 1. For each of following systems, y[n] denotes the output and x[n] the input. For each system, determine whether the specified input-output relationship is linear and/or shift-invariant.
 - (a) y[n] = 2x[n] + 3

(b)
$$y[n] = x[n]\sin\left(\frac{2\pi}{7}n + \frac{\pi}{6}\right)$$

- (c) $y[n] = (x[n])^3$
- (d) $y[n] = \sum_{m=n-N}^{n} x[m]$
- 2. Consider the sequence

$$x[n] = \begin{cases} a^n & n \ge n_0 \\ 0 & n < n_0 \end{cases}$$

- (a) Determine the z-transform of x[n].
- (b) Determine the Fourier transform of x[n]. Under what conditions does the Fourier transform exist?
- 3. Consider the first-order system, causal system,

$$y[n] = \alpha y[n-1] + x[n]$$

- (a) Find the system function, H[z], for this system.
- (b) Find the impulse response of this system.
- (c) For what values of α will the system be stable?
- (d) Assume that the input is obtained by sampling with period T . Determine the value of α such that

$$h[n] < e^{-1}$$
 for $nT > 2 m \sec$

i.e., find the value of α that gives a time constant of 2msec.

- 4. A speech signal is sampled at a rate of 10000 samples/sec(10 kHz). A segment of length 1024 samples is selected and the 1024-point DFT is computed.
 - (a) What is the time duration of segment of speech?
 - (b) What is the frequency resolution (spacing in Hz) between the DFT values?
 - (c) How do your answers to parts (a) and (b) change if we compute the 1024-point DFT of 512 samples of the speech signal. (The 512 samples would be augmented with 512 zero samples before the transform was computed.)